### Majorana Bound States in Semiconductor/Ferromagnetic insulator/Superconductor nanowire heterostructures

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Majorana Bound States (MBS) Motivation Outline

### **Ongoing work**



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Majorana Bound States (MBS) Motivation Outline

• MBS are topological subgap modes that can emerge at the ends of a superconductor/semiconductor nanowire

$$H = \begin{pmatrix} \frac{\hbar^2 k^2}{2m^*} - \mu + V_Z \sigma_x + \vec{\alpha} \cdot (\vec{\sigma} \times \vec{k}) \end{pmatrix} \tau_z - i\Delta \sigma_y \tau_y$$
  
Ingredients: Kinetic Electro-  
energy chemical potential SO Induced interaction superconductivity  
Zeeman field:  $V_Z = \frac{1}{2} \mu_B g B_x$ 



Majorana Bound States (MBS) Motivation Outline

• MBS are topological subgap modes that can emerge at the ends of a superconductor/semiconductor nanowire





• MBS may be useful for (topological) quantum computing.

T. Karzig et al., Phys. Rev. B 95, 235305 (2017)

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 MBS may be useful for (topological) quantum computing.

But the magnetic field weakens the superconductivity and complicates the scaling of a QC...

Y. Liu et al., ACS App. Mat. 12, 8780 (2020)

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 MBS may be useful for (topological) quantum computing. But the magnetic field weakens the superconductivity and complicates the scaling of a QC...

Is it possible to create MBS without a magnetic field?

Majorana Bound States (MBS) **Motivation** Outline

There is no need of an external magnetic field if it can be intrinsically incorporated. Recent experimental works show that it is possible to induce an exchange field in the nanowire by proximitizing an EuS layer to the heterostructure.



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Majorana Bound States (MBS) **Motivation** Outline

There is no need of an external magnetic field if it can be intrinsically incorporated. Recent experimental works show that it is possible to induce an exchange field in the nanowire by proximitizing an EuS layer to the heterostructure. This device shows ZBP compatible



Majorana Bound States (MBS) Motivation **Outline** 

Useful to understand the induced magnetization

Useful to study the phase diagram

- Realistic model ◄
  - Overlapping device
  - Non-overlapping device
- Effective model -
  - Overlapping device
  - Non-overlapping device
- Conclusions



We include in the Hamiltonian all the materials involved in the heterostructure using realistic parameters. We also include the self-consistent electrostatic environment.

$$H = \vec{k} \frac{\hbar^2}{2m_{\text{eff}}(\vec{r})} \vec{k} + E_{\text{F}}(\vec{r}) - e\phi(\vec{r}) + h_{\text{ex}}(\vec{r})\sigma_x + \Delta(\vec{r})\tau_x\sigma_x + \frac{1}{2} \left[ \vec{\alpha}(\vec{r}) \cdot (\vec{\sigma} \times \vec{k}) + (\vec{\sigma} \times \vec{k}) \cdot \vec{\alpha}(\vec{r}) \right]$$

Model

Results



Model Results

- Overlapping device
- Non-overlapping device

We compute the energy spectrum versus the momentum  $k_z$  for the **overlapping device** fixing all the gates to  $V_i=0$ . From there, we also compute the DOS. We perform three different simulations.



Model Results

- Overlapping device
- Non-overlapping device



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M. Rouko et al., Phys. Rev. B 100, 184501 (2019)

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We perform exactly the same simulations but for the **non-overlapping device**.



### 7

# Realistic model

### We perform exactly the same simulations but for the **non-overlapping device**.



Model Results

- Overlapping device
- Non-overlapping device

### We perform exactly the same simulations but for the **non-overlapping device**.





There is no topological phase in the nonoverlapping device, at least for this gate voltage

For the non-overlapping device, the induced exchange field seems not to be large enough to close the gap

#### Model Results

- Overlapping device
- Non-overlapping device

#### 7

## Realistic model

We perform exactly the same simulations but for the **non-overlapping device**.



Model **Results** 

- Overlapping device
- Non-overlapping device

### Effective model

Model Results

- Overlapping device
- Non-overlapping device

We "integrate out" the AI and the EuS, and we directly include the proximity effects into the InAs nanowire in an effective way. This reduces the computational cost and allows to find the phase diagram.



We compute the induced magnetization and superconductivity. We choose  $W_{sc}$  and  $W_{ex}$  in such a way to reproduce (roughly) the same behaviour as in the realistic model.

### Effective model

Model Results

- Overlapping device
- Non-overlapping device

We "integrate out" the AI and the EuS, and we directly include the proximity effects into the InAs nanowire in an effective way. This reduces the computational cost and allows to find the phase diagram.



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(EuS)

۲ ۷<sub>R</sub>

h<sub>ex</sub>

### Effective model

Model **Results** 

- **Overlapping device**
- Non-overlapping device

Δ

 $V_{\scriptscriptstyle L}$ 

Phase diagram vs  $V_{bg}$  (fixing V<sub>L</sub>=0 and V<sub>R</sub>=-4V) for an overlapping device with direct-induced magnetization



(AI)

'ex





(EuS)

۲ ۷<sub>R</sub>

h<sub>ex</sub>

### Effective model

Model **Results** 

Overlapping device

(AI)

Ъγ

Non-overlapping device

Δ

 $V_{\scriptscriptstyle L}$ 















# Conclusions and outlook

### Conclusions

- InAs/Al/EuS heterostructures intrinsically incorporates the effect of a Zeeman field large enough so that they can support MBS.
- Only some specific geometries give rise to MBS, because the wavefunction needs to be close to the EuS-InAs and Al-InAs interfaces at the same time. This can be controlled by the gates.

### Outlook

- How does the MBS wavefunction look like in finite-size nanowires? And their energies?
- How do they compare with experimental data?

For any question or inquire, don't hesitate to contact me via email at **samuel.diaz@uam.es**, thank you for your attention!

### **Supplementary Material**

### A: Effective Model

**Electrostatic potential** Induced superconductivity Induced Zeeman field

The electrostatic potential is determined self-consistently (in the Thomas-Fermi approximation) using the Poisson equation. The electrostatic environment is taken into account through the dielectric permittivity.



A recent experiment shows that there is an accumulation layer at the InAs-EuS interface similar to the one of the free facets. Thus, we include the same accumulation layer  $\rho_{acc}$  in the nanowire facets that are not in contact with Al. Additionally, we simulate the InAs-Al band bending imposing  $V_{sc}$  as boundary condition on the Al.

**Electrostatic potential** Induced superconductivity Induced Zeeman field

#### **Overlapping device**



As the back-gate voltage is increased, the wavefunction is pushed towards the bottom of the wire.

#### Non-overlapping device



**Electrostatic potential** Induced superconductivity Induced Zeeman field

#### **Overlapping device**



#### Non-overlapping device



Electrostatic potential Induced superconductivity Induced Zeeman field

To describe the superconductivity inside the semiconductor, one would need, in principle, to include the superconducting layer also at a tight-binding level.



Electrostatic potential Induced superconductivity Induced Zeeman field

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Electrostatic potential Induced superconductivity Induced Zeeman field

A different approach to include the proximity effect in the wire is to assume that a region of width  $W_{sc}$  close to the InAs/Al interface is characterized by a paring amplitude  $\Delta$ .



Using  $W_{sc}$ =30nm we predict a similar behaviour.

Electrostatic potential Induced superconductivity Induced Zeeman field

It is not clear how the magnetization induced by the EuS influences the state of the nanowire. There are two possible scenarios, which could be complementary.

### Model 1: direct-induced magnetization



The EuS **directly** induces an exchange field  $(h_{ex}^{(EuS)})$  in the InAs. Because the EuS is an insulator, the proximitized region is small (1nm), but with a large exchange field. In addition, it is known that there is a small exchange field  $(h_{ex}^{(Al)}=0.07\text{meV})$  in the Al due to the Al/EuS interface.

### Model 2: indirect-induced magnetization



The EuS induces an exchange field  $h_{ex}^{(Al)}$  in the InAs through the Al layer in an **indirect** way. The exchange field induced in the SC due to the Al-EuS interface is indeed, for whichever reason, larger than  $\Delta$ . The spinorbit coupling opens a gap even if the Clogston limit is reached.

Electrostatic potential Induced superconductivity Induced Zeeman field

To show that the first model is also plausible, let us describe first the EuS at a tight-binding level as well.



Electrostatic potential Induced superconductivity Induced Zeeman field

Although it is (computationally) affordable to include the EuS at a tight-binding layer, let us describe it as a proximitized region close to the InAs-EuS interface, as we did for the Al.



Using  $W_{Eus}$ =1nm and  $h_{ex}$  ~ 100meV we predict a similar behaviour.

### **Supplementary Material**

**Overlapping device** Non-overlapping device

• DOS vs  $V_{bg}$  for the **overlapping device** with  $h_{ex}=0$  and  $\alpha_{R}=0$ .





**Overlapping device** Non-overlapping device

• DOS vs  $V_{bg}$  for the **overlapping device** with  $h_{ex} \neq 0$  and  $\alpha_{R} = 0$ .



V<sub>bg</sub>=-3V V<sub>ba</sub>≈-1.5V V<sub>bq</sub>≈0V  $V_{bq}=1V$ 

**Overlapping device** Non-overlapping device

• DOS vs  $V_{bg}$  for the **overlapping device** with  $h_{ex} \neq 0$  and  $\alpha_{R} \neq 0$ .



V<sub>bq</sub>=-3V V<sub>ba</sub>≈-1.5V V<sub>bq</sub>≈0V  $V_{bq} = 1V$ W V Z\*₩ ¶ ¶ A A A  $\neg M$ 

**Overlapping device** Non-overlapping device





V<sub>bg</sub>=-3V V<sub>bq</sub>≈-1.5V V<sub>bq</sub>≈0V  $V_{bq}=1V$ 

Overlapping device **Non-overlapping device** 







### **Supplementary Material**

### C: 4-facets geometry

**Overlapping device** Non-overlapping device

V<sub>bq</sub>≈0V

• DOS vs  $V_{ba}$  for the **4-facets device** with  $h_{av} \neq 0$ and  $\alpha_{R}=0$ .



 $V_{ba} = 1V$ 

